

# IUU Fishing: Economic Effects of IUU Imports on U.S. Commercial Fishers

## Species: Sardine, Herring, Anchovies, Mackerel

*Model Release*

### Read Me :

This model accompanies the USITC report, *Seafood Obtained via Illegal, Unreported, and Unregulated Fishing: U.S. Imports and Economic Impact on U.S. Commercial Fisheries*, Inv. 332-575. The report includes a quantitative analysis of the economic impact of IUU imports on U.S. commercial fishers and U.S. commercial fishing production, trade, and prices. Economic effects are modeled by species, with each species-level model customized to fit the unique features of the U.S. domestic industry. Consumers of seafood products choose between domestic marine-capture sources, imports, and in some models, domestic aquaculture products. Imports include both legal and IUU sources that enter the U.S. at the same price, so consumers cannot distinguish an IUU from non-IUU product. 2018 data is used to establish an initial equilibrium with imports of IUU products included in the baseline. The model then removes the IUU imports, as estimated in chapter 3, and solves for a new equilibrium absent those products.

In the forage fish model, there are domestic and imported varieties of sardine, herring, anchovies, and mackerel species. The model includes cross-species substitution, so relative price changes in one species affects the other species. Annual catch limits (ACLs) are enforced in the model so modeled increases in domestic landings cannot exceed their legal limits. Catch limits are modeled as a vertical asymptote directly in the supply equation and not as a constraint.

There are two markets modeled: unprocessed and processed products. Landings flow to three destinations: the unprocessed market, the processed market, or are exported outside the country. The price of the processed product is a constant markup over the price of the unprocessed product, so increases in domestic prices of landed fish affect the price of processing. Initial consumption of unprocessed products, before the policy change was implemented, was calculated as a residual using 2018 conversion factors.

Data inputs in the simulation are in the BLUE-shaded cells (with sources for the input data listed in the cell above). Outputs are in the GREEN-shaded cells. The white cells are intermediate calculations.

Note:  $p_{xDU}$  is the price of the unprocessed product sold to consumers.  $q_{xDU}$  is the quantity of landings, not the unprocessed quantity sold to U.S. consumers. The unprocessed quantity sold to U.S. consumers must exclude exports and processed product \* conversion rate.

This PDF is a printout of the Mathematica file “IUU Fishing Model - forage fish - model release.nb”

*In[*<sup>®</sup>*]:= ClearAll[f];*

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## 1. Model Parameters

### 1.1 Within-Species Elasticity of Substitution

*Source: USITC's econometric estimation using the trade cost method in Riker (2020). More information can be found in the technical appendix (appendix I).*

**Unprocessed Sardine:** elasticity of substitution across varieties of unprocessed sardine

```
In[1]:= sigmasu = 6.57295 ;
```

**Processed Sardine:** elasticity of substitution across varieties of processed sardine

```
In[2]:= sigmasp = 6.57295 ;
```

**Unprocessed Herring:** elasticity of substitution across varieties of unprocessed herring

```
In[3]:= sigmahu = 7.794977 ;
```

**Processed Herring:** elasticity of substitution across varieties of processed herring

*In[*<sup>1</sup>*]:=* **sigmahp** = 7.794977;

**Unprocessed Anchovy:** elasticity of substitution across varieties of unprocessed anchovy

*In[*<sup>2</sup>*]:=* **sigmaau** = 5.863256;

**Processed Anchovy:** elasticity of substitution across varieties of processed anchovy

*In[*<sup>3</sup>*]:=* **sigmaap** = 5.863256;

**Unprocessed Mackerel:** elasticity of substitution across varieties of unprocessed mackerel

*In[*<sup>4</sup>*]:=* **sigmamu** = 7.794977;

**Processed Mackerel:** elasticity of substitution across varieties of processed mackerel

*In[*<sup>5</sup>*]:=* **sigmamp** = 7.794977;

## 1.2 Cross-Species Elasticity of Substitution

*Source: USITC Staff Estimate and Interviews with Industry Participants.*

**Unprocessed:** elasticity of substitution across unprocessed products

*In[*<sup>6</sup>*]:=* **betau** = 3.0;

**Processed:** elasticity of substitution across processed products

*In[*<sup>7</sup>*]:=* **betap** = 3.0;

## 1.3 Industry Price Elasticity of Demand

*Source: USITC Staff Estimate.*

**Unprocessed**

*In[*<sup>8</sup>*]:=* **etau** = -1.0;

**Processed**

*In[*<sup>9</sup>*]:=* **etap** = -1.0;

## 1.4 Illegal Imports Replacement Rates

*Source: USITC Staff Estimate. Further discussion on qualitative factors and rate determination can be found in appendix I of the USITC's report.*

**Sardine:** fraction of illegal imports replaced by legal imports of sardine

In[1]:= repls = 0.30;

**Herring:** fraction of illegal imports replaced by legal imports of herring

In[2]:= replh = 0.50;

**Anchovy:** fraction of illegal imports replaced by legal imports of anchovy

In[3]:= repla = 0.50;

**Mackerel:** fraction of illegal imports replaced by legal imports of mackerel

In[4]:= replm = 0.30;

## 1.5 Price Elasticity of Supply

Source: USITC Staff Estimate and Interviews with Industry Participants.

### U.S. landings of Sardine

In[5]:= esd = 1.0;

### U.S. landings of Herring

In[6]:= ehd = 2.0;

### U.S. landings of Anchovy

In[7]:= ead = 5.0;

### U.S. landings of Mackerel

In[8]:= emd = 5.0;

## 1.6 Conversion Factors

Source: Conversion factors were obtained from NOAA Fisheries

In[9]:= cr = 1.0;

## 2. Data Inputs

### 2.1 U.S. Landings Quantities and Prices

Source: National Oceanic and Atmospheric Administration. National Marine Fisheries Service (NOAA Fisheries). Fisheries of the United States 2018. Current Fishery Statistics No. 2018. U.S. Department of Commerce. Silver Spring MD: NOAA, February 2020. <https://www.fisheries.noaa.gov/resource/document/fisheries-united-states-2018-report>.

**Sardine**

*In[ ]:=*  $qsdu0 = 1,005,000; (*kg*)$

*In[ ]:=*  $psdu0 = 0.44776119; (*$/kg*)$

**Herring**

*In[ ]:=*  $qhdu0 = 66,719,000; (*kg*)$

*In[ ]:=*  $phdu0 = 0.49371244; (*$/kg*)$

**Anchovy**

*In[ ]:=*  $qadu0 = 17,360,000; (*kg*)$

*In[ ]:=*  $padu0 = 0.11388249; (*$/kg*)$

**Mackerel**

*In[ ]:=*  $qmdu0 = 87,333,209; (*kg*)$

*In[ ]:=*  $pmdu0 = 0.90390598; (*$/kg*)$

## 2.2 U.S. Processing Production Quantities and Prices

**Sources:**

National Oceanic and Atmospheric Administration. National Marine Fisheries Service (NOAA Fisheries). Fisheries of the United States 2018. Current Fishery Statistics No. 2018. U.S. Department of Commerce. Silver Spring MD: NOAA, February 2020. <https://www.fisheries.noaa.gov/resource/document/fisheries-united-states-2018-report>.

National Oceanic and Atmospheric Administration. National Marine Fisheries Service (NOAA Fisheries). NOAA Processed Products database. Accessed September 1, 2020.<https://www.fisheries.noaa.gov/foss/f?p=215:3:5412288074334::NO::>

**Processed Sardine**

*In[ ]:=*  $qsdp0 = 42,925; (*kg*)$

*In[ ]:=*  $psdp0 = 1.1706711; (*$/kg*)$

**Processed Herring**

*In[ ]:=*  $qhdp0 = 2,857,406; (*kg*)$

*In[ ]:=*  $phdp0 = 1.1706713; (*$/kg*)$

### Processed Anchovy

*In[6]:=*  $qadp0 = 7,229,685; (*kg*)$

*In[7]:=*  $padp0 = 0.4867994; (*$/kg*)$

### Processed Mackerel

*In[8]:=*  $qmfp0 = 40,331,122; (*kg*)$

*In[9]:=*  $pmfp0 = 3.0128494; (*$/kg*)$

## 2.3 Import Quantities and Prices

*Source: IUU Estimate Database as described in Chapter 3 of the report.*

### Sardine

Total unprocessed imports

*In[10]:=*  $qstu0 = 14,991,943; (*kg*)$

*In[11]:=*  $pstu0 = 0.641524; (*$/kg*)$

Total processed imports

*In[12]:=*  $qstp0 = 35,602,018; (*kg*)$

*In[13]:=*  $pstp0 = 4.17392; (*$/kg*)$

Illegal imports

*In[14]:=*  $qsiu0 = 2,943,611; (*kg*)$

*In[15]:=*  $qsip0 = 7,470,902; (*kg*)$

### Herring

Total unprocessed imports

*In[16]:=*  $qhtu0 = 2,459,463; (*kg*)$

*In[17]:=*  $phtu0 = 1.50032; (*$/kg*)$

Total processed imports

*In[18]:=*  $qhtp0 = 11,509,060; (*kg*)$

*In[*<sup>0</sup>*]:= phtp0 = 3.75706; (\*\$/kg\*)*

Illegal imports

*In[*<sup>0</sup>*]:= qhiu0 = 176,774; (\*kg\*)*

*In[*<sup>0</sup>*]:= qhip0 = 799,269; (\*kg\*)*

## Anchovy

Total unprocessed imports

*In[*<sup>0</sup>*]:= qatu0 = 1,761,278; (\*kg\*)*

*In[*<sup>0</sup>*]:= patu0 = 2.39253; (\*\$/kg\*)*

Total processed imports

*In[*<sup>0</sup>*]:= qatp0 = 4,890,903; (\*kg\*)*

*In[*<sup>0</sup>*]:= patp0 = 8.04725; (\*\$/kg\*)*

Illegal imports

*In[*<sup>0</sup>*]:= qaiu0 = 249,603; (\*kg\*)*

*In[*<sup>0</sup>*]:= qaip0 = 797,667; (\*kg\*)*

## Mackerel

Total unprocessed imports

*In[*<sup>0</sup>*]:= qmtu0 = 12,751,352; (\*kg\*)*

*In[*<sup>0</sup>*]:= pmtu0 = 2.76512; (\*\$/kg\*)*

Total processed imports

*In[*<sup>0</sup>*]:= qmtp0 = 20,583,069; (\*kg\*)*

*In[*<sup>0</sup>*]:= pmtp0 = 3.63618; (\*\$/kg\*)*

Illegal imports

*In[*<sup>0</sup>*]:= qmiu0 = 1,575,693; (\*kg\*)*

*In[8]:= qmip0 = 3,350,876; (\*kg\*)*

Calculation of legal imports

*In[9]:= qslu0 = qstu0 - qsiu0;*

*In[10]:= qslp0 = qstp0 - qsip0;*

*In[11]:= qhlu0 = qhtu0 - qhiu0;*

*In[12]:= qhlp0 = qhtp0 - qhip0;*

*In[13]:= qalu0 = qatu0 - qaiu0;*

*In[14]:= qalp0 = qatp0 - qaip0;*

*In[15]:= qmlu0 = qmtu0 - qmiu0;*

*In[16]:= qmlp0 = qmtp0 - qmip0;*

## 2.4 Export Quantities

*Source: National Oceanic and Atmospheric Administration. National Marine Fisheries Service (NOAA Fisheries). NOAA US Trade in Fishery Products database. Accessed September 1, 2020. <https://foss.nmfs.noaa.gov/apexfoss/f?p=215:2:14884747663545::NO>*

*In[17]:= qsdue0 = 0; (\*kg\*)*

*In[18]:= qsdpe0 = 0; (\*kg\*)*

*In[19]:= qhdue0 = 24,393,816; (\*kg\*)*

*In[20]:= qhdpe0 = 70,366; (\*kg\*)*

*In[21]:= qadue0 = 976,448; (\*kg\*)*

*In[22]:= qadpe0 = 920,018; (\*kg\*)*

*In[23]:= qmdue0 = 44,884,808; (\*kg\*)*

*In[24]:= qmdpe0 = 19,330; (\*kg\*)*

## 2.5 Catch Limits

### Sardine

*Source: 82 Fed. Reg. 29776 (June 30, 2018)*

*In[25]:= qsdcap = 8,000,000; (\*kg\*)*

## Herring

No aggregate ACL available, inserted arbitrarily high limit so it doesn't affect calculation.

```
In[1]:= qhdcap = 200,000,000; (*kg*)
```

## Anchovy

Source: Pacific Fishery Management Council, "Annual Season Management," accessed November 19, 2020. <https://www.pcouncil.org/current-season-management/>

```
In[2]:= qadcap = 34,750,000; (*kg*)
```

## Mackerel

Source: Aggregated several ACLs for jack, Atlantic, chub, king, Spanish, and atka mackerel species.

```
In[3]:= qmdcap = 180,605,093; (*kg*)
```

## 2.6 Import Market Share Statistics

Imports percent in market for unprocessed sardine

```
In[4]:= N[qsttu0 / (qsttu0 + (qsdu0 - qsdue0 - cr qsdp0))]
```

```
Out[4]= 0.939697
```

Imports percent in market for processed sardine

```
In[5]:= N[qstp0 / (qstp0 + (qsdp0 - qsdpe0))]
```

```
Out[5]= 0.998796
```

Imports percent in market for unprocessed herring

```
In[6]:= N[qhtu0 / (qhtu0 + (qhdu0 - qhdue0 - cr qhdp0))]
```

```
Out[6]= 0.0586603
```

Imports percent in market for processed herring

```
In[7]:= N[qhtp0 / (qhtp0 + (qhdp0 - qhdpe0))]
```

```
Out[7]= 0.805049
```

Imports percent in market for unprocessed anchovy

```
In[8]:= N[qatu0 / (qatu0 + (qadu0 - qadue0 - cr qadp0))]
```

```
Out[8]= 0.161361
```

Imports percent in market for processed anchovy

```
In[9]:= N[qatp0 / (qatp0 + (qadp0 - qadpe0))]
```

```
Out[9]= 0.436666
```

Imports percent in market for unprocessed mackerel

```
In[1]:= N[qmtu0 / (qmtu0 + (qmdu0 - qmdue0 - cr qmdp0)) ]
Out[1]= 0.857601
```

Imports percent in market for processed mackerel

```
In[2]:= N[qmtp0 / (qmtp0 + (qmdp0 - qmdpe0)) ]
Out[2]= 0.33801
```

### 3. Calibration

Baseline values of unprocessed and processed apparent consumption and imports

```
In[1]:= vstu0 = qstu0 pstu0;
In[2]:= vstp0 = qstp0 pstp0;
In[3]:= vhtu0 = qhtu0 phtu0;
In[4]:= vhtp0 = qhtp0 phtp0;
In[5]:= vatuo = qatu0 patuo;
In[6]:= vatp0 = qatp0 patp0;
In[7]:= vmtu0 = qmtu0 pmtu0;
In[8]:= vmtp0 = qmtp0 pmtp0;
In[9]:= vsdu0 = (qsdu0 - qsdue0 - cr qsdp0) psdu0;
In[10]:= vsdp0 = (qsdp0 - qsdpe0) psdp0;
In[11]:= vhdu0 = (qhdu0 - qhdue0 - cr qhdp0) phdu0;
In[12]:= vhdp0 = (qhdp0 - qhdpe0) phdp0;
In[13]:= vaduo = (qaduo - qadue0 - cr qadp0) paduo;
In[14]:= vadp0 = (qadp0 - qadpe0) padp0;
In[15]:= vmdu0 = (qmdu0 - qmdue0 - cr qmdp0) pmdu0;
In[16]:= vmdp0 = (qmdp0 - qmdpe0) pmdp0;
```

#### 3.1 Supply Parameters

```
In[1]:= esdu = N[esd qsdu0 / (qsdcap - qsdu0)];
In[2]:= asdu = (qsdcap - qsdu0) psdu0esdu;
In[3]:= ehdu = N[ehd qhdu0 / (qhdcap - qhdu0)];
In[4]:= ahdu = (qhdcap - qhdu0) phdu0ehdu;
```

```

ln[=]:= eadu = N[ead qadu0 / (qadcap - qadu0)];
ln[=]:= aadu = (qadcap - qadu0) padu0eadu;
ln[=]:= emdu = N[emd qmdu0 / (qmdcap - qmdu0)];
ln[=]:= amdu = (qmdcap - qmdu0) pmdu0emdu;

```

### 3.2 Demand Parameters

```

ln[=]:= bstu = vstu0 (pstu0 / psdu0)sigmasu-1;
ln[=]:= Psu0 = (psdu01-sigmasu + bstu pstu01-sigmasu)1/1-sigmasu;
ln[=]:= bhtu = vhtu0 (phtu0 / phdu0)sigmahu-1;
ln[=]:= Phu0 = (phdu01-sigmahu + bhtu phtu01-sigmahu)1/1-sigmahu;
ln[=]:= batu = vatu0 (patu0 / padu0)sigmaau-1;
ln[=]:= Pau0 = (padu01-sigmaau + batu patu01-sigmaau)1/1-sigmaau;
ln[=]:= bmtu = vmtu0 (pmtu0 / pmdu0)sigmamu-1;
ln[=]:= Pmu0 = (pmdu01-sigmamu + bmtu pmtu01-sigmamu)1/1-sigmamu;
ln[=]:= bhu = vhdu0 + vhtu0 (Phu0 / Psu0)betau-1;
ln[=]:= bau = vadu0 + vatu0 (Pau0 / Psu0)betau-1;
ln[=]:= bmu = vmdu0 + vmtu0 (Pmu0 / Psu0)betau-1;
ln[=]:= Pu0 = (Psu01-betau + bhu Phu01-betau + bau Pau01-betau + bmu Pmu01-betau)1/1-betau;
ln[=]:= bstp = vstp0 (pstp0 / psdp0)sigmasp-1;
ln[=]:= Psp0 = (psdp01-sigmasp + bstp pstp01-sigmasp)1/1-sigmasp;
ln[=]:= bhtp = vhtp0 (phtp0 / phdp0)sigmaph-1;
ln[=]:= Php0 = (phdp01-sigmahp + bhtp phtp01-sigmahp)1/1-sigmahp;

```

```

ln[=]:= batp =  $\frac{vatp\theta}{vadp\theta} \left( \frac{patp\theta}{padp\theta} \right)^{\text{sigmaap}-1};$ 
ln[=]:= Pap\theta =  $(padp\theta^{1-\text{sigmaap}} + batp patp\theta^{1-\text{sigmaap}})^{\frac{1}{1-\text{sigmaap}}};$ 
ln[=]:= bmtp =  $\frac{vmtp\theta}{vmdp\theta} \left( \frac{pmtp\theta}{pmdp\theta} \right)^{\text{sigmamp}-1};$ 
ln[=]:= Pmp\theta =  $(pmdp\theta^{1-\text{sigmamp}} + bmtp pmtp\theta^{1-\text{sigmamp}})^{\frac{1}{1-\text{sigmamp}}};$ 
ln[=]:= bhp =  $\frac{vhdp\theta + vhtp\theta}{vsdp\theta + vstp\theta} \left( \frac{Php\theta}{Psp\theta} \right)^{\text{betap}-1};$ 
ln[=]:= bap =  $\frac{vadp\theta + vatp\theta}{vsdp\theta + vstp\theta} \left( \frac{Pap\theta}{Psp\theta} \right)^{\text{betap}-1};$ 
ln[=]:= bmp =  $\frac{vmdp\theta + vmtp\theta}{vsdp\theta + vstp\theta} \left( \frac{Pmp\theta}{Psp\theta} \right)^{\text{betap}-1};$ 
ln[=]:= Pp\theta =  $(Psp\theta^{1-\text{betap}} + bhp Php\theta^{1-\text{betap}} + bap Pap\theta^{1-\text{betap}} + bmp Pmp\theta^{1-\text{betap}})^{\frac{1}{1-\text{betap}}};$ 
ln[=]:= ku =  $\frac{qstu\theta Pu\theta^{-\text{etau}-\text{betau}} Psu\theta^{\text{betau}-\text{sigmasu}} pstu\theta^{\text{sigmasu}}}{bstu};$ 
ln[=]:= kp =  $\frac{qstp\theta Pp\theta^{-\text{etap}-\text{betau}} Psp\theta^{\text{betap}-\text{sigmasp}} pstp\theta^{\text{sigmasp}}}{bstp};$ 

```

## 4. New Equilibrium Calculation

```

ln[=]:= Psu =  $(psdu^{1-\text{sigmasu}} + bstu pstu^{1-\text{sigmasu}})^{\frac{1}{1-\text{sigmasu}}};$ 
ln[=]:= Phu =  $(phdu^{1-\text{sigmahu}} + bhtu phtu^{1-\text{sigmahu}})^{\frac{1}{1-\text{sigmahu}}};$ 
ln[=]:= Pau =  $(padu^{1-\text{sigmaau}} + batu patu^{1-\text{sigmaau}})^{\frac{1}{1-\text{sigmaau}}};$ 
ln[=]:= Pmu =  $(pmdu^{1-\text{sigmamu}} + bmtu pmtu^{1-\text{sigmamu}})^{\frac{1}{1-\text{sigmamu}}};$ 
ln[=]:= Pu =  $(Psu^{1-\text{betau}} + bhu Phu^{1-\text{betau}} + bau Pau^{1-\text{betau}} + bmu Pmu^{1-\text{betau}})^{\frac{1}{1-\text{betau}}};$ 
ln[=]:= psdp =  $\frac{psdu psdp\theta}{psdu\theta};$ 
ln[=]:= phdp =  $\frac{phdu phdp\theta}{phdu\theta};$ 
ln[=]:= padp =  $\frac{padu padp\theta}{padu\theta};$ 
ln[=]:= pmdp =  $\frac{pmdu pmdp\theta}{pmdu\theta};$ 
ln[=]:= Psp =  $(psdp^{1-\text{sigmasp}} + bstp pstp^{1-\text{sigmasp}})^{\frac{1}{1-\text{sigmasp}}};$ 

```

$$\begin{aligned} \ln[j]:= \mathbf{Php} &= \left( \mathbf{phdp}^{1-\text{sigmahp}} + \mathbf{bhtp} \mathbf{phtp}^{1-\text{sigmahp}} \right)^{\frac{1}{1-\text{sigmahp}}}; \\ \ln[j]:= \mathbf{Pap} &= \left( \mathbf{padp}^{1-\text{sigmaap}} + \mathbf{batp} \mathbf{patp}^{1-\text{sigmaap}} \right)^{\frac{1}{1-\text{sigmaap}}}; \\ \ln[j]:= \mathbf{Pmp} &= \left( \mathbf{pmdp}^{1-\text{sigmamp}} + \mathbf{bmtp} \mathbf{pmtp}^{1-\text{sigmamp}} \right)^{\frac{1}{1-\text{sigmamp}}}; \\ \ln[j]:= \mathbf{Pp} &= \left( \mathbf{Psp}^{1-\text{betap}} + \mathbf{bhp} \mathbf{Php}^{1-\text{betap}} + \mathbf{bap} \mathbf{Pap}^{1-\text{betap}} + \mathbf{bmp} \mathbf{Pmp}^{1-\text{betap}} \right)^{\frac{1}{1-\text{betap}}}; \end{aligned}$$

### Equilibrium equations

Supply (landings) of sardine = exports + consumer demand for unprocessed fish + consumer demand for processed fish

$$\ln[j]:= \mathbf{E1} = \mathbf{qsdcap} - \mathbf{asdu} \mathbf{psdu}^{-\text{esdu}} = \mathbf{qsdue0} + \mathbf{cr} \mathbf{qsdpe0} + \mathbf{ku} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Psu}^{\text{sigmasu}-\text{betau}} \mathbf{psdu}^{-\text{sigmasu}} + \mathbf{cr} \mathbf{kp} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Psp}^{\text{sigmasp}-\text{betap}} \mathbf{psdp}^{-\text{sigmasp}};$$

Supply (landings) of herring = exports + consumer demand for unprocessed fish + consumer demand for processed fish

$$\ln[j]:= \mathbf{E2} = \mathbf{qhdcap} - \mathbf{ahdu} \mathbf{phdu}^{-\text{ehdu}} = \mathbf{qhdue0} + \mathbf{cr} \mathbf{qhdpe0} + \mathbf{ku} \mathbf{bhu} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Phu}^{\text{sigmahu}-\text{betau}} \mathbf{phdu}^{-\text{sigmahu}} + \mathbf{cr} \mathbf{bhp} \mathbf{kp} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Php}^{\text{sigmahp}-\text{betap}} \mathbf{phdp}^{-\text{sigmahp}};$$

Supply (landings) of anchovy = exports + consumer demand for unprocessed fish + consumer demand for processed fish

$$\ln[j]:= \mathbf{E3} = \mathbf{qadcap} - \mathbf{aadu} \mathbf{padu}^{-\text{eadu}} = \mathbf{qadue0} + \mathbf{cr} \mathbf{qadpe0} + \mathbf{ku} \mathbf{bau} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Pau}^{\text{sigmaau}-\text{betau}} \mathbf{padu}^{-\text{sigmaau}} + \mathbf{cr} \mathbf{bap} \mathbf{kp} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Pap}^{\text{sigmaap}-\text{betap}} \mathbf{padp}^{-\text{sigmaap}};$$

Supply (landings) of mackerel = exports + consumer demand for unprocessed fish + consumer demand for processed fish

$$\ln[j]:= \mathbf{E4} = \mathbf{qmdcap} - \mathbf{amdu} \mathbf{pmdu}^{-\text{emd}} = \mathbf{qmdue0} + \mathbf{cr} \mathbf{qmdpe0} + \mathbf{ku} \mathbf{bmu} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Pmu}^{\text{sigmamu}-\text{betau}} \mathbf{pmdu}^{-\text{sigmamu}} + \mathbf{cr} \mathbf{bmp} \mathbf{kp} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Pmp}^{\text{sigmamp}-\text{betap}} \mathbf{pmdp}^{-\text{sigmamp}};$$

Supply of imported unprocessed product = Demand for imported unprocessed product

$$\ln[j]:= \mathbf{E5} = \mathbf{qslu0} + \mathbf{rep1s} \mathbf{qsiu0} = \mathbf{ku} \mathbf{bstu} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Psu}^{\text{sigmasu}-\text{betau}} \mathbf{pstu}^{-\text{sigmasu}};$$

$$\ln[j]:= \mathbf{E6} = \mathbf{qhlu0} + \mathbf{rep1h} \mathbf{qhiu0} = \mathbf{ku} \mathbf{bhtu} \mathbf{bhu} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Phu}^{\text{sigmahu}-\text{betau}} \mathbf{phtu}^{-\text{sigmahu}};$$

$$\ln[j]:= \mathbf{E7} = \mathbf{qalu0} + \mathbf{rep1a} \mathbf{qaiu0} = \mathbf{ku} \mathbf{batu} \mathbf{bau} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Pau}^{\text{sigmaau}-\text{betau}} \mathbf{patu}^{-\text{sigmaau}};$$

$$\ln[j]:= \mathbf{E8} = \mathbf{qmlu0} + \mathbf{rep1m} \mathbf{qmip0} = \mathbf{ku} \mathbf{bmtu} \mathbf{bmu} \mathbf{Pu}^{\text{etau}+\text{betau}} \mathbf{Pmu}^{\text{sigmamu}-\text{betau}} \mathbf{pmtu}^{-\text{sigmamu}};$$

Supply of imported processed product = Demand for imported processed product

$$\ln[j]:= \mathbf{E9} = \mathbf{qslp0} + \mathbf{rep1s} \mathbf{qrip0} = \mathbf{kp} \mathbf{bstp} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Psp}^{\text{sigmasp}-\text{betap}} \mathbf{pstp}^{-\text{sigmasp}};$$

$$\ln[j]:= \mathbf{E10} = \mathbf{qhlp0} + \mathbf{rep1h} \mathbf{qhip0} = \mathbf{kp} \mathbf{bhtp} \mathbf{bhp} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Php}^{\text{sigmahp}-\text{betap}} \mathbf{phtp}^{-\text{sigmahp}};$$

$$\ln[j]:= \mathbf{E11} = \mathbf{qalp0} + \mathbf{rep1a} \mathbf{qaip0} = \mathbf{kp} \mathbf{batp} \mathbf{bap} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Pap}^{\text{sigmaap}-\text{betap}} \mathbf{patp}^{-\text{sigmaap}};$$

$$\ln[j]:= \mathbf{E12} = \mathbf{qmlp0} + \mathbf{rep1m} \mathbf{qmip0} = \mathbf{kp} \mathbf{bmtp} \mathbf{bmp} \mathbf{Pp}^{\text{etap}+\text{betap}} \mathbf{Pmp}^{\text{sigmamp}-\text{betap}} \mathbf{pmtp}^{-\text{sigmamp}};$$

```

In[1]:= FindRoot[{E1, E2, E3, E4, E5, E6, E7, E8, E9, E10, E11, E12}, {psdu, psdu0}, {pstu, pstu0},
  {phdu, phdu0}, {phtu, phtu0}, {padu, padu0}, {patu, patu0}, {pmdu, pmdu0},
  {pmtu, pmtu0}, {pstp, pstp0}, {phtp, phtp0}, {patp, patp0}, {pmtp, pmtp0}]

Out[1]= {psdu → 0.469825, pstu → 0.693184, phdu → 0.502316, phtu → 1.54259,
  padu → 0.116306, patu → 2.51206, pmdu → 0.915281, pmtu → 2.9239,
  pstp → 4.54554, phtp → 3.91521, patp → 8.52724, pmtp → 3.79292}

In[2]:= psdu1 = psdu /. %;

In[3]:= pstu1 = pstu /. %%;

In[4]:= pstp1 = pstp /. %%%;

In[5]:= phdu1 = phdu /. %%%%;

In[6]:= phtu1 = phtu /. %%%%%;

In[7]:= phtp1 = phtp /. %%%%%%;

In[8]:= padu1 = padu /. %%%%%%%;

In[9]:= patu1 = patu /. %%%%%%%;

In[10]:= patp1 = patp /. %%%%%%%;

In[11]:= pmdu1 = pmdu /. %%%%%%%;

In[12]:= pmtu1 = pmtu /. %%%%%%%;

In[13]:= pmtp1 = pmtp /. %%%%%%%;

In[14]:= psdp1 =  $\frac{psdu1 \cdot psdp0}{psdu0}$ ;

In[15]:= phdp1 =  $\frac{phdu1 \cdot phdp0}{phdu0}$ ;

In[16]:= padp1 =  $\frac{padu1 \cdot padp0}{padu0}$ ;

In[17]:= pmdp1 =  $\frac{pmdu1 \cdot pm dp0}{pmdu0}$ ;

In[18]:= Psu1 =  $(psdu1^{1-sigmasu} + bstu \cdot pstu1^{1-sigmasu})^{\frac{1}{1-sigmasu}}$ ;

In[19]:= Phu1 =  $(phdu1^{1-sigmahu} + bhtu \cdot phtu1^{1-sigmahu})^{\frac{1}{1-sigmahu}}$ ;

In[20]:= Pau1 =  $(padu1^{1-sigmaau} + batu \cdot patu1^{1-sigmaau})^{\frac{1}{1-sigmaau}}$ ;

In[21]:= Pmu1 =  $(pmdu1^{1-sigmamu} + bmtu \cdot pmtu1^{1-sigmamu})^{\frac{1}{1-sigmamu}}$ ;

In[22]:= Pu1 =  $(psu1^{1-betau} + bhu \cdot phu1^{1-betau} + bau \cdot pau1^{1-betau} + bmu \cdot pmu1^{1-betau})^{\frac{1}{1-betau}}$ ;

In[23]:= Psp1 =  $(psdp1^{1-sigmasp} + bstp \cdot pstp1^{1-sigmasp})^{\frac{1}{1-sigmasp}}$ ;

```

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ln[=]:= Php1 =  $(\text{phdp1}^{1-\text{sigmahp}} + \text{bhtp phtp1}^{1-\text{sigmahp}})^{\frac{1}{1-\text{sigmahp}}};$ 
ln[=]:= Pap1 =  $(\text{padp1}^{1-\text{sigmaap}} + \text{batp patp1}^{1-\text{sigmaap}})^{\frac{1}{1-\text{sigmaap}}};$ 
ln[=]:= Pmp1 =  $(\text{pmdp1}^{1-\text{sigmamp}} + \text{bmtp pmtp1}^{1-\text{sigmamp}})^{\frac{1}{1-\text{sigmamp}}};$ 
ln[=]:= Pp1 =  $(\text{Psp1}^{1-\text{betap}} + \text{bhp Php1}^{1-\text{betap}} + \text{bap Pap1}^{1-\text{betap}} + \text{bmp Pmp1}^{1-\text{betap}})^{\frac{1}{1-\text{betap}}};$ 
ln[=]:= qsdu1 = qsdcap - asdu psdu1^-esdu;
ln[=]:= qstu1 = qslu0 + repls qsiu0;
ln[=]:= qstp1 = qslp0 + repls qsip0;
ln[=]:= qsdp1 = qsdpe0 + kp Pp1^etap+betap Psp1^sigmasp-betap pmdp1^-sigmasp;
ln[=]:= qhdu1 = qhdcap - ahdu phdu1^-ehdu;
ln[=]:= qhtu1 = qhlu0 + replh qhiu0;
ln[=]:= qhtp1 = qhlp0 + replh qhip0;
ln[=]:= qhdp1 = qhdpe0 + kp bhp Pp1^etap+betap Php1^sigmahp-betap phdp1^-sigmahp;
ln[=]:= qadu1 = qadcap - aadu padu1^-eadu;
ln[=]:= qatu1 = qalu0 + repla qaiu0;
ln[=]:= qatp1 = qalp0 + repla qaip0;
ln[=]:= qadp1 = qadpe0 + kp bap Pp1^etap+betap Pap1^sigmaap-betap padp1^-sigmaap;
ln[=]:= qmdu1 = qmdcap - amdu pmdu1^-emdus;
ln[=]:= qmtu1 = qmlu0 + replm qmiu0;
ln[=]:= qmtp1 = qmlp0 + replm qmip0;
ln[=]:= qmdp1 = qmdpe0 + kp bmp Pp1^etap+betap Pmp1^sigmamp-betap pmdp1^-sigmamp;

```

## 5. Results

### Sardines

Percent change in price of unprocessed domestic sardine production

$$\frac{(\text{psdu1} - \text{psdu0}) 100}{\text{psdu0}}$$

Out[=]=

4.92756

Percent change in quantity of domestic sardine landings

$$\ln[f]:= \frac{(qsdu1 - qsdu0) 100}{qsdu0}$$

Out[ $\#$ ]:= 4.79342

Change in landings (in kg)

$$\ln[f]:= qsdu1 - qsdu0$$

Out[ $\#$ ]:= 48,173.8

Percent change in price of processed domestic production

$$\ln[f]:= \frac{(psdp1 - psdp0) 100}{psdp0}$$

Out[ $\#$ ]:= 4.92756

Percent change in quantity of processed domestic production

$$\ln[f]:= \frac{(qsdp1 - qsdp0) 100}{qsdp0}$$

Out[ $\#$ ]:= 8.93605

Change (\$) in operating income, unprocessed product

$$\ln[f]:= (1 / \text{sigmasu}) (psdu1 (qsdu1 - qsdue0 - cr qsdp1) - psdu0 (qsdu0 - qsdue0 - cr qsdp0))$$

Out[ $\#$ ]:= 6398.65

Change (\$) in operating income, processed product

$$\ln[f]:= (1 / \text{sigmasp}) (psdp1 (qsdp1 - qsdpe0) - psdp0 (qsdp0 - qsdpe0))$$

Out[ $\#$ ]:= 1093.55

Percent change in price of unprocessed imports

$$\ln[f]:= \frac{(pstu1 - pstu0) 100}{pstu0}$$

Out[ $\#$ ]:= 8.0527

Percent change in quantity of unprocessed imports

$$\ln[f]:= \frac{(qstu1 - qstu0) 100}{qstu0}$$

Out[ $\#$ ]:= -13.7442

Percent change in price of processed imports

$$\ln[\text{]:= } \frac{(pstp1 - pstp0) 100}{pstp0}$$

*Out[ ]:=* 8.90347

Percent change in quantity of processed imports

$$\ln[\text{]:= } \frac{(qstp1 - qstp0) 100}{qstp0}$$

*Out[ ]:=* -14.6891

## Herring

Percent change in price of unprocessed domestic herring production

$$\ln[\text{]:= } \frac{(phdu1 - phdu0) 100}{phdu0}$$

*Out[ ]:=* 1.74255

Percent change in quantity of domestic herring landings

$$\ln[\text{]:= } \frac{(qhdu1 - qhdu0) 100}{qhdu0}$$

*Out[ ]:=* 3.42537

Change in landings (in kg)

$$\ln[\text{]:= } qhdu1 - qhdu0$$

*Out[ ]:=*  $2.28537 \times 10^6$

Percent change in price of processed domestic production

$$\ln[\text{]:= } \frac{(phdp1 - phdp0) 100}{phdp0}$$

*Out[ ]:=* 1.74255

Percent change in quantity of processed domestic product

$$\ln[\text{]:= } \frac{(qhdःp1 - qhdःp0) 100}{qhdःp0}$$

*Out[ ]:=* 15.9444

Change (\$) in operating income, unprocessed product

$In[6]:= \frac{(1/\text{sigmahu}) (\text{phdu1} (\text{qhdu1} - \text{qhdue0} - \text{cr qhd}p1) - \text{phdu0} (\text{qhdu0} - \text{qhdue0} - \text{cr qhd}p0))}{161,472.}$

Change (\$) in operating income, processed product

$In[7]:= \frac{(1/\text{sigmaph}) (\text{phdp1} (\text{qhd}p1 - \text{qhd}pe0) - \text{phdp0} (\text{qhd}p0 - \text{qhd}pe0))}{76,908.5}$

Percent change in price of unprocessed imports

$$In[8]:= \frac{(\text{phtu1} - \text{phtu0}) 100}{\text{phtu0}}$$

$Out[8]= 2.8174$

Percent change in quantity of unprocessed imports

$$In[9]:= \frac{(\text{qhtu1} - \text{qhtu0}) 100}{\text{qhtu0}}$$

$Out[9]= -3.59375$

Percent change in price of processed imports

$$In[10]:= \frac{(\text{phtp1} - \text{phtp0}) 100}{\text{phtp0}}$$

$Out[10]= 4.20946$

Percent change in quantity of processed imports

$$In[11]:= \frac{(\text{qhtp1} - \text{qhtp0}) 100}{\text{qhtp0}}$$

$Out[11]= -3.47235$

## Anchovy

Percent change in price of unprocessed domestic anchovy production

$$In[12]:= \frac{(\text{padu1} - \text{padu0}) 100}{\text{padu0}}$$

$Out[12]= 2.12819$

Percent change in quantity of domestic anchovy landings

$$\ln[f]:= \frac{(qadu1 - qadu0) 100}{qadu0}$$

Out[ $\#$ ]:= 9.99482

Change in landings (in kg)

$$\ln[f]:= qadu1 - qadu0$$

Out[ $\#$ ]:=  $1.7351 \times 10^6$

Percent change in price of processed domestic production

$$\ln[f]:= \frac{(padp1 - padp0) 100}{padp0}$$

Out[ $\#$ ]:= 2.12819

Percent change in quantity of processed domestic product

$$\ln[f]:= \frac{(qadp1 - qadp0) 100}{qadp0}$$

Out[ $\#$ ]:= 12.2311

Change (\$) in operating income, unprocessed product

$$\ln[f]:= (1 / \sigma_{aa}) (padu1 (qadu1 - qadue0 - cr qadp1) - padu0 (qadu0 - qadue0 - cr qadp0))$$

Out[ $\#$ ]:= 20,661.2

Change (\$) in operating income, processed product

$$\ln[f]:= (1 / \sigma_{ap}) (padp1 (qadp1 - qadpe0) - padp0 (qadp0 - qadpe0))$$

Out[ $\#$ ]:= 86,128.4

Percent change in price of unprocessed imports

$$\ln[f]:= \frac{(patu1 - patu0) 100}{patu0}$$

Out[ $\#$ ]:= 4.99597

Percent change in quantity of unprocessed imports

$$\ln[f]:= \frac{(qatu1 - qatu0) 100}{qatu0}$$

Out[ $\#$ ]:= -7.08585

Percent change in price of processed imports

$$\ln[\text{]:= } \frac{(p\text{atp1} - p\text{atp0}) 100}{p\text{atp0}}$$

*Out[ ]:=* 5.96468

Percent change in quantity of processed imports

$$\ln[\text{]:= } \frac{(q\text{atp1} - q\text{atp0}) 100}{q\text{atp0}}$$

*Out[ ]:=* -8.1546

### Mackerel

Percent change in price of unprocessed domestic mackerel production

$$\ln[\text{]:= } \frac{(p\text{mdu1} - p\text{mdu0}) 100}{p\text{mdu0}}$$

*Out[ ]:=* 1.25841

Percent change in quantity of domestic mackerel landings

$$\ln[\text{]:= } \frac{(q\text{mdu1} - q\text{mdu0}) 100}{q\text{mdu0}}$$

*Out[ ]:=* 6.07327

Change in landings (in kg)

$$\ln[\text{]:= } q\text{mdu1} - q\text{mdu0}$$

*Out[ ]:=*  $5.30398 \times 10^6$

Percent change in price of processed domestic production

$$\ln[\text{]:= } \frac{(p\text{mdp1} - p\text{mdp0}) 100}{p\text{mdp0}}$$

*Out[ ]:=* 1.25841

Percent change in quantity of processed domestic product

$$\ln[\text{]:= } \frac{(q\text{mdp1} - q\text{mdp0}) 100}{q\text{mdp0}}$$

*Out[ ]:=* 11.6784

Change (\$) in operating income, unprocessed product

$$\text{In[1]:= } N[(1/\text{sigmamu}) (\text{pmdu1} (\text{qmdu1} - \text{qmdue0} - \text{cr qmdp1}) - \text{pmdu0} (\text{qmdu0} - \text{qmdue0} - \text{cr qmdp0}))]$$

Out[1]= 72,830.8

Change (\$) in operating income, processed product

$$\text{In[2]:= } N[(1/\text{sigmamp}) (\text{pmdp1} (\text{qmdp1} - \text{qmdp0}) - \text{pmdp0} (\text{qmdp0} - \text{qmdp0}))]$$

Out[2]=  $2.03946 \times 10^6$

Percent change in price of unprocessed imports

$$\text{In[3]:= } \frac{(\text{pmtu1} - \text{pmtu0}) 100}{\text{pmtu0}}$$

Out[3]= 5.74218

Percent change in quantity of unprocessed imports

$$\text{In[4]:= } \frac{(\text{qmtu1} - \text{qmtu0}) 100}{\text{qmtu0}}$$

Out[4]= -8.64995

Percent change in price of processed imports

$$\text{In[5]:= } \frac{(\text{pmtip1} - \text{pmtip0}) 100}{\text{pmtip0}}$$

Out[5]= 4.31067

Percent change in quantity of processed imports

$$\text{In[6]:= } \frac{(\text{qmtip1} - \text{qmtip0}) 100}{\text{qmtip0}}$$

Out[6]= -11.3958

## Price Indexes

Percent change in unprocessed price index

$$\text{In[7]:= } \frac{(\text{Pu1} - \text{Pu0}) 100}{\text{Pu0}}$$

Out[7]= 4.56925

Percent change in processed price index

$$\ln f = \frac{(Pp1 - Pp0) \cdot 100}{Pp0}$$

Out[6]= 4.9725